

have adverse effects for the real economy. Borrower-based measures such as LTV limits could help to address these vulnerabilities. In addition to the existing capital based measures already implemented, the national authorities have drafted a legal framework for borrower-based measures to address risks related to household indebtedness in the residential real estate sector. Although the legal project for these instruments was transmitted to the Luxembourg Parliament in December 2017, they have not yet been formally adopted in the legislation. Nevertheless, there is a need to assess the optimal calibration of these instruments and they should be activated as soon as they are available in the national toolbox.

It is against this background that this study aims at addressing the following two interrelated questions: i) What would be the optimal loan-to-value (LTV) ratio/rule as a borrower-based macroprudential instrument for Luxembourg in a general equilibrium framework? This is an important policy issue as banks in Luxembourg currently implement various LTV ratios depending on their own assessment of household creditworthiness. ii) How important are the combinations of borrower and capital based macroprudential instruments and how can their optimal combination be determined?

To address these questions, this study proposes a framework for calibrating optimal macroprudential policies, assessing their interactions and evaluating their implications for financial stability. To this end, we build a DSGE model that features a housing sector and household debt dynamics. The model is estimated on Luxembourg data using Bayesian techniques. Unlike other studies in the literature, we distinguish between the flow and the stock of household debt in the model. We also introduce a monopolistically competitive banking sector, which features the costs of regulatory capital requirements and a feedback loop channel between the real and the financial side of the economy.

With respect to macroprudential policies, we introduce both borrower and capital based measures in order to determine their optimal ratios and interactions. We identify the optimal macroprudential ratios and rules for LTV and sectoral capital requirements while adopting a broad definition of the sectoral capital requirement that we call the risk weighted capital requirement (RW). We subsequently discuss the effectiveness of the optimal combination of instruments through their ability to stabilize the financial cycle, house prices and household indebtedness in the presence of both interest rate and LTV shocks. Finally, a welfare comparison of alternative policies is conducted in order to draw meaningful conclusions of the potential costs of these instruments to the real economy.

Our main findings can be summarized as follows⁸⁰. First, the non-joint optimal ratios of LTV and RW leading to the maximum social welfare are respectively found to be 90% and 30% for Luxembourg in the context of an easy monetary policy environment. When solely an LTV measure is applied, it should be too tight at 20% to be realistic, leading admittedly to a welfare loss but bringing about stabilized debt relative to the use of both LTV and RW ratios. Second, we find that combining a borrower based instrument, such as the LTV cap, with a capital based one, as the RW ratio, welfare-dominates the use of LTV alone. This result suggests that these two instruments can be considered as complements in terms of welfare improvement. Notably, a single LTV measure performs better than combining the two instruments in terms of mortgage debt and house prices stabilization effects. These results suggest that the policy scenario that provides better stabilization effects on mortgage credit growth isn't necessarily the one that is welfare improving. More precisely, we find a complementarity between LTV and RW in terms of welfare improvement, while their optimal combination deteriorates the stabilization effects on mortgage debt and house prices.

80 Note that the modelling framework used to generate the results does not take into account all features of the residential real estate market in Luxembourg. In particular the constraints on the residential real estate supply, public incentives, such as the tax deductibility of mortgage interest rate, are omitted from the model.

Nevertheless, the time-varying and endogenous rules for LTV and RW improves social welfare and better stabilizes mortgage loans and the house prices compared to their static exogenous ratios. Finally, we find that the optimal interactions between LTV and RW ratios in our modelling framework have a convex shape. In other words, when LTV increases, the corresponding optimal RW ratio decreases and conversely, when the RW ratio increases, the corresponding optimal LTV ratio decreases.


2 LITERATURE REVIEW

The existing studies using the DSGE modelling approach for analysing the Luxembourg economy specifically are limited. Deák et al. (2011) built a DSGE model called the LSM (Luxembourg Structural Model) which captures the main structural features of the Luxembourg economy in order to undertake various policy experiments. Marchiori and Pierrard (2017) proposed a general equilibrium model calibrated on the Luxembourg economy, which features overlapping generation dynamics and labour market frictions, with the purpose of assessing how global demand for financial services promotes domestic growth in Luxembourg. These authors do not model the housing and financial sector and do not address financial regulation issues in the context of their models.

This work is related to four strands of literature. First, it is related to numerous papers that model housing sector with borrowing constraints in a dynamic stochastic general equilibrium framework (e.g. Iacoviello (2005), Iacoviello and Neri (2010), Gerali et al. (2010), Mendicino and Punzi (2014), Rubio and Carrasco-Gallego (2014), Guerrieri and Iacoviello (2017)). However, few works among the mentioned papers explicitly model the banking sector. Brzoza-Brzezina et al. (2017) use a small open economy model with a shortcut of the banking sector for studying the role of foreign currency loans under monetary and macroprudential policy, but their model does not contain any frictions in the banking sector nor a distinction between the mortgage credit flow and stock. Gerali et al. (2010) do consider frictions in the banking sector but they do not differentiate between mortgage lending flow and stock. We try to fill this gap by considering a DSGE model in which banks are explicitly modelled in a monopolistic competitive market and mortgage loan stocks and flows are explicitly differentiated in the model.

This study is also related to the growing body of literature on macroprudential policies. Several previous papers have explored the effectiveness of macroprudential policies using dynamic stochastic general equilibrium models. In particular, Lubello and Rouabah (2017) use a DSGE model with a shadow banking sector that is calibrated on euro area data to assess the role of the macroprudential policy in mitigating the effects of both real and financial shocks. However, their calibrated model does not account for the housing sector. Fève and Pierrard (2017) recently tackled issues related to macroprudential regulation using an estimated DSGE model with a shadow banking sector but without a housing sector. Overall, few studies have been interested in exploring the optimality of macroprudential policies (Rubio and Carrasco-Gallego (2014), Mendicino and Punzi (2014), Punzi and Rabitsch (2018)). However none of these studies focus on the interaction between macroprudential instruments. Most of these papers analyse optimal interactions between the monetary policy and macroprudential policy using calibrated models rather than assessing the optimal interaction of macroprudential policies.

Our work fits into the literature on combinations of macroprudential instruments. This strand of the literature is growing and most studies address the combination of borrower based instruments using regression techniques (Kelly et al. (2018) and Albacete et al. (2018) among others). Some exceptions include Chen and Columba (2016), Grodecka (2017) and Greenwald (2018) who analysed the combination of borrower based instruments using a DSGE modelling approach. Fewer works investigate the combination between borrower and capital based instruments using the DSGE modelling approach. In



particular, Benes et al. (2016) use a DSGE model for studying the effectiveness of the countercyclical capital buffer and the LTV ratio but in the absence of any optimality analysis.

Finally, the literature on the explicit distinction between credit flow and debt stock has a connection with our work. As far as we know, there exist only three papers in this case, Kydland et al. (2016), Grodecka (2017) and Alpanda and Zubairy (2017). These authors investigate household indebtedness or the effectiveness of macroprudential instruments by distinguishing mortgage credit flow from debt stock. However, they do not model the banking sector contrary to what we are doing in this study. Unlike these authors, we precisely emphasize the traditional feedback loop between the financial and real sector by incorporating the banking sector à la Gerali et al. (2010) in our modelling approach.

3 MODEL

In this study, we consider a closed-economy DSGE model with a housing sector, a collateral constraint and household debt. Two groups of households populate the economy: patient households and impatient households. Patient households are savers and have higher discount factors than impatient households who are borrowers ($\beta_p > \beta_i$). This heterogeneity in agents' discount factors generates positive fund flows in equilibrium; patient households make positive deposits and do not borrow, while impatient households borrow a positive amount of loans. Patient households consume, work and accumulate capital and housing. Impatient households consume, work and accumulate housing. As impatient households are considered to be borrowers, they are constrained by having to collateralize the value of their net worth (a financial friction).

We introduce a monopolistically competitive banking sector à la Gerali et al. (2010) in the model. Banks intermediate the funds that flow from patient households to impatient households as they have different degrees of impatience. Banks issue loans to impatient households by collecting deposits from patient households and accumulating their own capital out of reinvested profits. A second financial friction is introduced in the model by assuming that banks are subject to a risk weighted capital requirement constraint that translates into an exogenous target for the leverage ratio and implies a quadratic cost. Unlike Gerali et al. (2010), we introduce a distinction between the mortgage credit flow and stock following Kydland et al. (2016) and Alpanda and Zubairy (2017).

On the production side, monopolistically competitive intermediate-goods-producing firms produce heterogeneous intermediate goods using physical capital, bought from capital goods producers, and labour supplied by households in return for sticky wages à la Calvo (1983). The prices of intermediate goods are also set in a staggered fashion à la Calvo (1983). Final goods-producing firms, who bundle intermediate goods into final goods, capital and housing producers operate in perfectly competitive markets.

Finally, a passive government covers its expenditures and transfers to households by issuing bonds that are purchased by savers and a monetary authority follows a standard Taylor-type interest rate rule.

We present here only a brief summary of the model. All model details including the first order conditions derived from agents' optimization programmes are available under request and in Sangaré (2019).

3.1 HOUSEHOLDS

There are two types of households in the economy, each of unit mass and indexed by “ I ” and “ P ”. Households derive utility from consumption ($c_{z,t}$), housing services ($h_{z,t}$) and hours worked, ($n_{z,t}$)⁸¹, where $z \in [I, P]$.

Patient households

The representative patient household “ i ” maximizes their expected utility function subject to the following budget constraint (in real terms):

$$\begin{aligned} c_{P,t}(i) + q_{h,t}[h_{P,t}(i) - (1 - \delta_h)h_{P,t-1}(i)] + q_{k,t}[k_t(i) - (1 - \delta_k)k_{t-1}(i)] + d_t(i) + b_t(i) \\ = w_{P,t}(i)n_{P,t}(i) + r_{k,t}k_{t-1}(i) + (1 + r_{t-1}) \left[\frac{d_{t-1}(i) + b_{t-1}(i)}{\Pi_t} \right] + tr_{P,t} \\ + \Lambda_t \end{aligned} \quad (1)$$

where $h_{P,t}$ and k_t are accumulated housing and physical capital with $q_{h,t}$ and $q_{k,t}$ their respective real prices. The stock of housing and physical capital depreciate at rates δ_h and δ_k , respectively. d_t defines real deposits made in the period and b_t is the real amount of one-period government bonds purchased by patient households, on which they earn a gross nominal interest rate of $(1 + r_t)$. $\Pi_t = P_t/P_{t-1}$ defines the gross inflation rate with P_t as consumption goods prices. $r_{k,t}$ denotes the rental rate of physical capital received from the intermediate goods producing firms, while $w_{P,t}$ stands for the real wage. Patient households receive lump-sum transfers from government, $tr_{P,t}$, and dividends from monopolistically competitive firms and banks, Λ_t .

Impatient households

The representative impatient household “ i ” also maximizes the expected utility function subject to the following budget constraint:

$$\begin{aligned} c_{I,t}(i) + q_{h,t}[h_{I,t}(i) - (1 - \delta_h)h_{I,t-1}(i)] + (r_{M,t-1} + \kappa) \frac{de_{t-1}(i)}{\Pi_t} \\ = w_{I,t}(i)n_{I,t}(i) + l_t(i) + tr_{I,t} \end{aligned} \quad (2)$$

and the following collateral constraint

$$l_t(i) \leq m_{h,t} \left[\frac{(1 - \delta_h)E_t q_{h,t+1} h_{I,t}(i) \Pi_{t+1}}{(1 + r_{L,t})} - (1 - \kappa) \frac{de_{t-1}(i)}{\Pi_t} \right] \mu_{m,t} \quad (3)$$

where $h_{I,t}$ is housing accumulated by impatient households. The latter don't accumulate any physical capital and borrow, l_t , from banks at a gross nominal interest rate of $(1 + r_{L,t})$. They earn $w_{I,t}$ as wages and receive lump-sum transfers, $tr_{I,t}$, from government as for patient households.

81 The expected utility of the representative household of each type of household and the first order conditions derived from households' problem are detailed in Sangaré [2019].

$m_{h,t}$ denotes the loan-to-value (LTV) on total mortgage loans, and is set by the macroprudential authority. The collateral constraint (3) means impatient households cannot borrow more than a fraction of the expected value of their net wealth (the expected value of the housing stock minus the real value of non-amortized debt)⁸². $\mu_{m,t}$ defines an exogenous LTV shock which follows an autoregressive process AR(1).

$(r_{M,t-1} + \kappa) \frac{de_{t-1}(i)}{\Pi_t}$ represents impatient households (borrowers) mortgage payments, defined as the sum of interest and principal payments. $r_{M,t}$ denotes the effective interest rate on all mortgage outstanding and κ is the amortization rate determining the principal payments out of the stock of debt.

Therefore, the stock of mortgage debt evolves as according to:

$$de_t(i) = (1 - \kappa) \frac{de_{t-1}(i)}{\Pi_t} + l_t(i) \quad (4)$$

New and refinanced loans are both subject to the period interest rate $r_{L,t}$ set by the banks. Following Alpanda and Zubairy (2017), the effective interest rate is assumed to be:

$$r_{M,t} = (1 - \zeta) \left(1 - \frac{l_t}{de_t}\right) r_{M,t-1} + \left[\left(\frac{l_t}{de_t}\right) + \zeta \left(1 - \frac{l_t}{de_t}\right)\right] r_{L,t} \quad (5)$$

where the fraction of existing loans that are refinanced each period is ζ .

If $\zeta = 1$, all mortgage loans are refinanced and the effective rate equals the new loan rate ($r_{M,t} = r_{L,t}$), while when $\zeta = 0$ the model features no refinancing loans. Furthermore, note that if $\kappa = 1$ the model does not differentiate debt stock and loans ($l_t = de_t$) and we have one-period debt as common in the literature and the effective interest rate would again simply equal the banking new loan rate ($r_{M,t} = r_{L,t}$).

Wage setting

In order to introduce wage stickiness in the model, we assume that labour services are heterogeneous across households within each group, which gives households some pricing power in setting their own wages. These differentiated labour services are aggregated into a homogeneous labour service (using a Constant Elasticity of Substitution (CES) aggregator) by perfectly competitive labour intermediaries (called unions or labour packers), who in turn rent these labour services to goods producers. Following Calvo (1983), we assume that households are not freely able to adjust their wage each period. This assumption defines wage stickiness in the model.

3.2 BANKING SECTOR

The banking sector is built up of a continuum of banks $j \in [0,1]$. Following Gerali et al. (2010) and Gambacorta and Signoretti (2014), we assume that each bank (j) is composed of two segments: a wholesale branch and a retail branch.

The perfectly competitive wholesale segment collects deposits ($d_t(j)$) from patient households paying a net interest rate, r_t , set by the central bank and issues loans, $l_t(j)$, on which it earns the wholesale loan net rate. Furthermore, the bank has own funds $k_{b,t}(j)$, which are accumulated out of reinvested profits.

⁸² As in Iacoviello (2005), we assume that the shocks are small enough that the collateral constraint always binds.

Following Gerali et al. (2010), we assume that the bank has a target τ_t for their capital-to-assets ratio (i.e., the inverse of leverage ratio) and pays a quadratic cost whenever it deviates from that target. The target can be interpreted as an exogenous regulatory constraint that imposes the amount of own resources to hold. The existence of a cost for deviating from τ_t implies that the degree of bank leverage affects credit conditions in the economy. Wholesale bank (j)'s problem is therefore to maximize its profits subject to the following balance sheet constraint: $l_t(j) = d_t(j) + k_{b,t}(j)$.

The retail loan branch operates under monopolistic competition. This segment obtains loans from the wholesale segment, differentiates them at no cost and resells them to final borrowers (i.e., impatient households) at rate $r_{L,t}$. As in Gambacorta and Signoretti (2014), we assume that the retail loan rate ($r_{L,t}$) is set in the process by simply applying a constant mark-up m_b on the wholesale loan rate so that:

$$r_{L,t} = r_t - \chi \left(\frac{k_{b,t}(j)}{l_t(j)} - \tau_t \right) \left(\frac{k_{b,t}(j)}{l_t(j)} \right)^2 + m_b \quad (6)$$

3.3 CAPITAL AND HOUSING PRODUCERS

In each period, perfectly competitive capital investment-goods producers purchase last-period undepreciated capital from patient households and capital investment goods from final-goods firms at a relative price of one, and produce the new capital goods increasing the effective installed capital, which is then sold back to patient households. This transformation process is subject to adjustment costs in the change in investment. We assume that residential investment producers act in a way that is analogous to that of capital producers. Both capital and housing producers optimally behave by maximizing their profits.

3.4 GOODS PRODUCTION

Perfectly competitive final-goods producers purchase differentiated intermediate goods that are bundled into final goods via the Dixit-Stiglitz aggregator. A continuum of monopolistically competitive intermediate-goods producers $j \in [0,1]$, produce each intermediate good (j) according to the following production function:

$$y_t(j) = \mu_{y,t} (k_{t-1}(j))^\alpha \left[(n_{I,t}^d(j))^\eta (n_{P,t}^d(j))^{1-\eta} \right]^{1-\alpha} \quad (7)$$

where α is the share of capital in overall production, and η denotes the share of impatient households in the labour input. $n_{P,t}^d(j)$ and $n_{I,t}^d(j)$ represent labour supplied by patient and impatient households. $\mu_{y,t}$ is the sector wide total factor productivity which follows an AR(1) process.

Firms solve their cost minimization problem subject to (7), which provides the real cost of production factors. Price rigidities are introduced in the model following the New Keynesian literature. Firms are subject to Calvo price-setting and the optimal price is found by solving their dynamic problem of profit maximization.

3.5 GOVERNMENT AND MONETARY POLICY

The government finances its exogenous consumption and transfers to households by issuing debt. The central bank sets monetary policy according to the Taylor-type rule.

3.6 MARKET CLEARING CONDITIONS

The model's equilibrium is defined as a set of prices and allocations such that households maximize the discounted present value of utility, banks maximize the discount present value of profits, and all firms maximize the discounted present value of profits subject to their constraints, and all markets clear.

4 ESTIMATION

The model was estimated using Bayesian methods and Luxembourg data. We estimate the structural parameters that mainly affect the model dynamics and calibrate the parameters that either determine the steady state so as to match key statistics in the data or are non-identifiable. In the section that follows, we first discuss the calibrated parameters, the priors and data and we then report the parameter estimates.

4.1 CALIBRATION AND PRIORS

Table 1 reports the values of the calibrated parameters. The parameters are set in such a way that the model matches the economic data for Luxembourg. The steady state gross inflation rate is set to 1.005, corresponding to the average long-run annual inflation rate of 2% in Luxembourg. We set the discount factor of patient households, β_P , at 0.999 in order to match the average annual Euribor rate of 2.1% in our sample (1999-2017). As for the discount factor of impatient households', β_I , we set it at 0.995 corresponding to the average annual spread between the Euribor rate and loan rates on new mortgage contracts in Luxembourg of 190 bps.

The capital share in output, α , is calibrated at 0.3, corresponding to the share of labour income over GDP of 0.7 as per Luxembourg data. The capital depreciation rates in the residential (δ_h) and non-residential (δ_k) sectors are set respectively at 0.005 and 0.01 corresponding to residential and non-residential investments over their respective stock of capital in the data. The relative weight of housing in the utility function, χ_h , is calibrated such that the ratio of housing over consumption in the steady state is 0.043.

Setting the weight of labour in utility, χ_n , to 7 allows us to match the share of working time of 1/3. The steady-state LTV ratio, m_h , is set at 0.7 consistent with the average data. The steady state value of capital-to-mortgage loan ratio (τ) is calibrated as 0.25 as provided by the Luxembourg end-period data (2017).

We calibrate the amortization rate for mortgage loans, κ , at 0.0165, which implies that the average duration of mortgage loans in the model is 20 years⁸³. This value is consistent with Luxembourg data. Given this value and the ratio of debt stock to flow in the data, we infer that the share of loans that is refinanced in the model, ζ , is about 0.02, by assuming that the refinancing share of the first loan applications in data is small (10%) as there are no available Luxembourg data on this parameter.

83 Following Alpanda and Zubairy (2017), we approximate the duration by 2 times the half-life of the loan.

Some steady state ratios are required for solving the models. Bank's capital-to-GDP ratio is set at 3% according to the end-period data. Public debt-to-GDP and spending-to-GDP ratios are respectively 23% and 20% as per the average data in the sample.

Parameters for which data are not available to calibrate are set following the literature. We calibrate the share of impatient households' income in labour income, η , at 0.7, following Alpanda and Zubairy (2017) and the fact that the BCL survey of Luxembourg households (HFCS, 2014) reports a small share of income of wealthier households (top deciles) over the total income declared.

All other parameters are estimated. The prior distributions are reported in Table 2. Our choices of prior distributions follow the literature and some theoretical restrictions. In particular, a Beta distribution is chosen for the parameters restricted to the interval $[0, 1]$, Gamma and Normal distributions are chosen for the parameters which are assumed to be positive and an Inverse-Gamma distribution is used for the standard deviation of shocks. The prior means and standard errors are closely chosen from the literature.

4.2 DATA

We use the following 8 observable series for the estimation: real private consumption, real house price index, real residential investment, real non-residential investment, domestic households' mortgage debt stock, total hours worked, CPI inflation rate, and the Euribor interest rate (6 months). The real residential investment in data is defined by the dwellings gross fixed capital formation and the gross fixed capital formation excluding dwellings denotes the real non-residential investment. Data series are collected quarterly and the sample period is 1999Q-2017Q4. Series with seasonal patterns are seasonally adjusted by the Census X-12 procedure and those with trend are HP-filtered in order to make them stationary, while both the interest and inflation rate are demeaned.

4.3 POSTERIOR ESTIMATES

The posterior distributions of the parameters are obtained using the Metropolis-Hastings algorithm with 2 chains of 200 000 draws. The acceptance rate by chain was 0.25. Convergence was assessed by the convergence statistics proposed by Brooks and Gelman (1998). Table 2 reports the mean and the 5th and 95th percentiles of the posterior distributions of the estimated parameters. Clearly, it appears that data are quite informative about most of the parameters and the parameter estimates are in line with the literature.

Table 1:

Calibrated parameters

β_P	Discount factor of patient households	0.999
β_I	Discount factor of impatient households	0.995
α	Capital share in output	0.3
δ_h	Residential capital depreciation rate	0.005
δ_k	Non-residential capital depreciation rate	0.01
χ_h	Weight of housing in the utility	0.3
χ_n	Weight of labour in utility	7
m_h	LTV ratio	0.7
τ	Capital-to-asset ratio	0.25
κ	Amortization rate	0.0165
ζ	Share of refinanced loans	0.02
k_b/Y	Capital-to-GDP ratio	0.03
b/Y	Public debt-to-GDP ratio	0.23
G/Y	Public spending-to-GDP ratio	0.2
η	Share of Impatients in labour income	0.7

Source: *Calculs BCL*.

Table 2:

Estimated parameters

PARAMETER	DESCRIPTION	PRIOR DISTRIBUTION			POSTERIOR DISTRIBUTION	
		DISTRIBUTION	MEAN	SD	MEAN	95% INTERVAL
α	Habit in consumption	Beta	0.4	0.02	0.5077	[0.4782 0.5296]
ϕ	Inverse of Frisch elasticity	Gamma	1	0.15	1.1585	[0.8368 1.4704]
θ	Calvo wage stickiness	Beta	0.85	0.1	0.337	[0.2426 0.4370]
ψ	Calvo price stickiness	Beta	0.85	0.1	0.6577	[0.6109 0.7039]
ϵ_w	Labour substitution elasticity	Gamma	6	1.5	4.1131	[2.0805 6.2955]
ϵ	Goods substitution elasticity	Gamma	6	1.5	5.6797	[3.9188 7.6730]
ξ_k	Capital investment adj. cost	Gamma	2	1.5	0.2165	[0.1531 0.2841]
ξ_h	Housing investment adj. cost	Gamma	2	1.5	0.287	[0.2009 0.3831]
χ	Bank leverage deviation cost	Normal	1	0.1	0.6582	[0.4818 0.8565]
γ_1	Taylor rule smoothing coeff.	Beta	0.8	0.1	0.6758	[0.5943 0.7496]
γ_2	Taylor rule coeff. on inflation	Normal	2.2	0.15	2.4582	[2.2154 2.7015]
γ_3	Taylor rule coeff. on output	Normal	0.04	0.01	0.0476	[0.0293 0.0668]
ρ_c	AR consumption pref. shock	Beta	0.5	0.15	0.5765	[0.3888 0.7535]
ρ_h	AR housing pref. shock	Beta	0.5	0.15	0.7006	[0.6324 0.7696]
ρ_y	AR productivity shock	Beta	0.5	0.15	0.2162	[0.1054 0.3303]
ρ_r	AR monetary policy shock	Beta	0.5	0.15	0.1606	[0.0612 0.2651]
ρ_q	AR LTV shock	Beta	0.5	0.15	0.0684	[0.0187 0.1233]
ρ_k	AR capital invest. shock	Beta	0.5	0.15	0.4109	[0.3402 0.4806]
ρ_{hi}	AR housing invest. shock	Beta	0.5	0.15	0.9802	[0.9634 0.9947]
ρ_g	AR gov. spending shock	Beta	0.5	0.15	0.8618	[0.8179 0.9035]
σ_c	SD consumption pref. shock	Inv. gamma	0.001	0.1	0.1277	[0.0958 0.1635]
σ_h	SD housing pref. shock	Inv. gamma	0.001	0.1	0.9404	[0.6940 1.2005]
σ_y	SD productivity shock	Inv. gamma	0.001	0.1	0.0855	[0.0647 0.1075]
σ_r	SD monetary policy shock	Inv. gamma	0.001	0.1	0.0058	[0.0045 0.0071]
σ_q	SD LTV shock	Inv. gamma	0.001	0.1	0.2952	[0.2447 0.3475]
σ_k	SD capital invest. shock	Inv. gamma	0.001	0.01	0.5055	[0.3880 0.6258]
σ_{hi}	SD housing invest. shock	Inv. gamma	0.001	0.1	2.0861	[1.6924 2.5122]
σ_g	SD gov. spending shock	Inv. gamma	0.001	0.1	0.7573	[0.5868 0.9233]

Source: *Calculs BCL*.

5 MACROPRUDENTIAL INSTRUMENTS AND THE OPTIMAL POLICY FRAMEWORK

In this section, we discuss the instruments and the objectives of the macroprudential authority. We consider two macroprudential instruments: loan-to-value (LTV) and the sectoral capital requirement⁸⁴. This includes all capital requirements that target the mortgage sector, including regulatory risk weights, countercyclical capital requirements affecting mortgage loans and other broad-based capital measures on banks, etc...⁸⁵. For simplicity, we interpret this broad sectoral capital requirement

⁸⁴ Note that the current model allows for taking into account another macroprudential tool, which is the amortization requirement. To make the analysis more tractable, we only focus on the two mentioned instruments in the current study and we plan to analyse the amortization requirement in the future work.

⁸⁵ We refer to this as the shares of capital charges on banks that could weigh on mortgage lending, keeping in mind that all broad regulatory capital requirements might affect the mortgage loan sector.

as risk weights (RW) on mortgage loans with the additional assumption that all risks born by the bank stem from the mortgage sector. We choose these instruments because of their direct impacts on housing demand and prices and the policy need to assess the combinations of borrower and capital-based instruments. Therefore, our instruments capture the two key aspects of the macroprudential policy namely the demand and supply sides of mortgage loans.

In general, macroprudential policies in standard DSGE models consist of exogenously setting macroprudential instruments at fixed values, which are not time varying as they are not affected by economic conditions. In this work, we first take into account these types of static ratios and we further extend the model by introducing the macroprudential policy rules for the two aforementioned tools.

5.1 MACROPRUDENTIAL POLICY INSTRUMENTS

5.1.1 Static ratios

We start by looking at the policy case where both the instruments (LTV and RW) are exogenous and defined as fixed parameters. We then find the optimal values of these LTV and RW ratios. The optimality criteria will be defined later.

5.1.2 Dynamic and endogenous rules

In this section we assume that LTV and RW measures are not static but dynamic and endogenous in the sense that they depend on some endogenous variables of the model, as described below.

LTV rule

As in Kannan et al. (2012) and Rubio and Carrasco-Gallego (2014), we assume that a regulatory macroprudential policy for LTV (denoted as $m_{h,t}$ is time varying and a of Taylor-type rule so that it reacts inversely to the credit-to-GDP gap, in the spirit of the Basel III regulation which aims at addressing episodes of excessive credit growth:

$$m_{h,t} = m_{h,op} - \phi_l \widehat{\Delta}_t \quad (8)$$


Here $m_{h,op}$ is the optimal static level of LTV, $\widehat{\Delta}_t$ denotes the mortgage loan-to-GDP gap and ϕ_l measures the response of the LTV requirement to the gap. With this kind of rule, LTV would be set low in booms, restricting credit to the housing sector and therefore avoiding a mortgage boom stemming from economic upswings (and conversely for economic downturns).

Sectoral risk weighted rule

The risk weighted capital requirement rule (RW) is a time varying Taylor-type rule reacting to a key macroeconomic variable as in Angelini et al. (2012). We choose this variable to be the cyclical component of output. The risk weighted capital requirement (denoted by τ_t) is then set according to the following rule:

$$\tau_t = \tau_{op} - \chi_\tau \widehat{y}_t \quad (9)$$

where τ_{op} measures the optimal static level of the RW requirement, \widehat{y}_t represents the cyclical component of output (i.e., a proxy for the output gap) and χ_τ denotes the response parameter of capital requirements to the business cycle. A positive value of χ_τ stands for a countercyclical policy: capital



requirements increase during economic upswings (i.e. banks hold more capital for a given mortgage loan) and decrease in recessions. This capital requirement rule is in line with the countercyclical capital buffer introduced by Basel III.

5.2 AN OPTIMAL MACROPRUDENTIAL POLICY FRAMEWORK

An optimal policy analysis aims at identifying optimal values for the policy ratios or reaction parameters which could maximize the objective function of the macroprudential authority. Therefore, determining the optimal policy calibration requires defining the objective of the macroprudential/financial stability authority and then the optimality criteria.

It is challenging to model the objectives of macroprudential policies within a DSGE framework since vulnerabilities in the financial system can arise from different sectors in various forms. Furthermore, there is no specific proxy or widely accepted definition of such policy objectives in the majority of macro models.

Given the commonly accepted definition of the objective of the macroprudential authority, which is to safeguard financial stability, some authors such as Rubio and Carrasco-Galego (2014) and Angelini et al. (2012) assume that there exists a loss function for the macroprudential authority. This loss function is assumed to depend on a set of weighted variable volatilities that is minimized subject to the equilibrium conditions of the model. This approach is similar to the one of the optimal monetary policy in which the monetary policy authority minimizes its loss function.

However, using loss functions in a DSGE context is generally a short-cut approach to the social welfare analysis. The reason is that the loss function is derived from the second order approximation to the expected utility function of the representative household in the basic New Keynesian (NK) model in the absence of real and financial frictions (with only price stickiness)⁸⁶. The authority's loss function therefore represents an average welfare loss and depends on the variability of some endogenous variables⁸⁷. Moreover, the economic rationale behind the use of the welfare loss function as a policy objective function, which depends on the volatilities of variables, is that the volatility has an impact on the welfare of economic agents. For example, from a financial stability perspective, lower volatility of credit growth can help to smooth borrowers' consumption and therefore improves their welfare.

For these reasons, we use a welfare based approach in this work and the maximization of the social welfare as a proxy for the objective of the macroprudential authority. We therefore define the optimal macroprudential policy as the one that maximise the social welfare of the economy. Rather than using a weighted sum of volatilities as the macroprudential authority's loss function (like in Rubio and Carrasco-Galego (2014) and Angelini et al. (2012)), which is equivalent to the analytically derived welfare loss only in a basic NK model without real and financial frictions, we numerically compute the social welfare losses/gains since our model is far more complex than the basic NK model. We perform a grid search for values of macroprudential ratios and parameters of instruments that maximise the social welfare.

We compute the welfare loss/gain for each type of economic agent under each policy regime using optimal ratios and optimized rule parameters. This facilitates an evaluation of the benefits of implementing

⁸⁶ See for instance, Gali (2008), Gali and Monacelli (2005, 2008).

⁸⁷ The monetary policy authority's loss function depends for instance on the variability of both the output gap and the rate of inflation [See Gali (2008) for more details].

different macroprudential policies. We follow Schmitt-Grohe and Uribe (2007) by computing the conditional welfare of agents using the second order approximation of the model (and rules).

To make the welfare results more intuitive, we define a welfare metric in terms of consumption equivalents. This consumption equivalent welfare measure is the constant fraction of steady-state consumption that households are willing to give away in order to obtain the benefits of the macroprudential policy. A positive value means a welfare gain, which is how much the consumer would be willing to pay in terms of steady-state consumption to obtain a welfare improvement.

6 OPTIMAL VALUES OF LTV AND RW AND THE DYNAMIC OF THE MODEL

In this section, we first present the optimal macroprudential ratios and optimal parameters for the rules along the lines of the concepts presented in the previous section. Afterwards, we discuss the dynamics of the model.

In this sense, we address an important policy question, among other things, of what would be the optimal ratios for LTV and RW and optimal parameters for the Taylor-type macroprudential rules in Luxembourg?

The results are discussed in the context of a loose monetary policy environment and a LTV shock. A second order approximation is used for solving the model and providing the quantitative results⁸⁸.

6.1 OPTIMAL LTV AND RW RATIOS AND OPTIMIZED PARAMETERS OF THE POLICY RULES

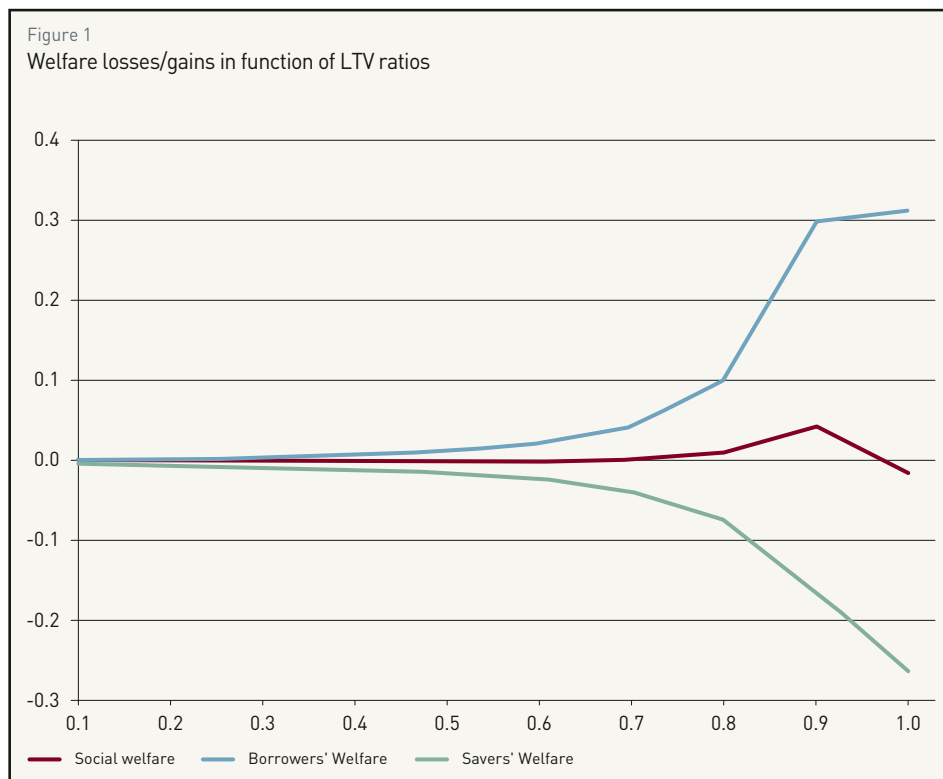
We start by computing volatilities and welfare losses/gains for the scenario in which LTV and RW are set to their average values based on the data (i.e. the benchmark case). Afterwards, we report the results for a single instrument scenario (LTV alone), a two-instrument scenario (LTV and RW) and a scenario in which the model comprises the optimal rules for instruments.

Table 3 shows the optimal ratios, optimal parameter values of policy rules, volatilities and the welfare gains/losses for different policy scenarios in a low interest rate environment. Note that when the two instruments are both used in the policy framework we assume that the set-up of the optimization exercise consists of searching for the optimal value of each ratio or rule's parameter while taking the other as given and set to its value based on the data. This is the non-joint optimization. The joint optimal values of the ratios from the joint optimization perspective are provided later.

When the two instruments are both used in the economy model (Column 3), the optimal static LTV ratio is found to be 90% while the optimal RW ratio is about 30%. These optimal levels imply a welfare gain for borrowers while savers face a welfare loss. Social welfare is therefore positive as a consequence of the welfare gain from the borrowers' side. The intuition is as follows: on one hand, increasing the LTV ratio has a direct effect on borrowers' welfare as the collateral constraint is loosened. However, up to a certain threshold, borrowers could be over-indebted as higher consumption levels imply higher interest rates (inflation being increased). This leads to higher repayments, which act to curb consumption and welfare levels.

⁸⁸ Second order approximation methods have the particular advantage of accounting for effects of volatility of variables on the mean levels. See among others Schmitt-Grohe and Uribe (2004).

Figure 1
Welfare losses/gains in function of LTV ratios



Source: *Calculs BCL.*

On the other hand, higher interest rates imply higher returns on saving and, as the savers' intertemporal optimization determines their consumption pattern, they reduce their consumption. This channel is reinforced by the increase in the inflation rate following the increase in loans to borrowers (higher LTV). These results are illustrated in Figure 1.

If the RW ratio is removed from the authority's macroprudential toolkit, meaning that there are no capital requirements weighing on the banking sector, the scenario of a single LTV policy (Column 2) provides a tighter optimal value of 0.2 for the LTV ratio. This means the LTV ratio, used alone, may need to be tightened in a loose monetary policy environment, which can result in relatively low volatilities of credit and output while generating a welfare loss for the economy.

Even if this scenario is less realistic in practice, it allows for assessing synergies and complementarities between LTV and RW measures in the context of the model.

Comparing the two-instrument policy scenario to the one with a single LTV policy, Table 3 (Benchmark Column and Column 3) shows that mortgage lending and output are less stabilized in the former than the latter case. However, the two-instrument policy implies a social welfare gain for the economy while the single LTV policy scenario provides a social welfare loss, suggesting that the two macroprudential instruments (LTV and RW) are complements in terms of welfare effects. The welfare gain of the combination of two instruments is around 1.2% in terms of consumption equivalents.

These results suggest that the policy scenario that provides a better stabilization of mortgage loans is not necessarily the one that is welfare improving. In particular, the implementation of both LTV and RW measures generates higher macro financial volatilities relative to a LTV only policy regime. This is explained by the fact that the collateral channel effects stemming from an optimal tighter LTV worsens borrowers' welfare as they are more constrained to borrow and then to consume. The LTV ratio used in a single policy scenario should optimally be tight if facing a low interest rate environment, as it restricts and stabilises credit flows to borrowers and decreases or stabilizes their consumption and wealth effects from house acquisition on consumption fall. The presence of both the borrower- and capital-based instruments in the macroprudential toolkit, i.e., one (LTV) on the credit demand side and the other (RW) on the price side (i.e. loan rates leads to a higher LTV depending on the fixation of the RW ratio). Figure 2 shows that the welfare characterisation is jointly dependent on LTV and RW with the welfare effects being somewhat convex. When the optimal RW ratio increases, the optimal ratio of LTV corresponding to the highest value of welfare is low and conversely, when the LTV

increases the corresponding optimal RW decreases. Therefore, the joint optimal value of LTV and RW are respectively 100% and 10% as illustrated by the elevated region (in blue) in Figure 2.

We finally compare the outcomes from the static LTV and RW ratios to those under time varying rules. We find that introducing the time-varying macroprudential rules is welfare improving with an associated welfare gain of 0.43% compared to the case of the static ratios. Moreover, in terms of macro financial stabilization, mortgage lending and output are more stabilized under the time-varying policy rule scenario than under the static ratio scenario. The two-instrument rule provides better outcomes in terms of volatilities and welfare suggesting the interest of introducing such rules.

The results in terms of stabilisation of output and credit flows are consistent with the impulse response functions presented below.

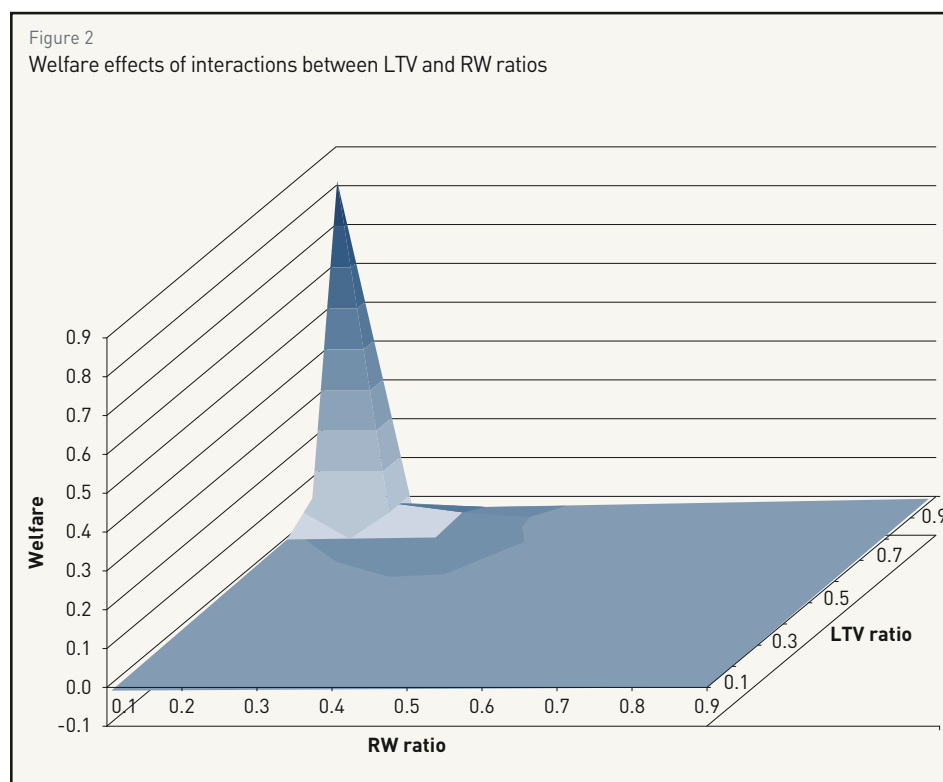
Table 3:

Optimal LTV and RW policies

	BENCHMARK	OPTIMAL STATIC POLICY		OPTIMAL POLICY RULES
		SINGLE INSTRUMENT	TWO INSTRUMENTS	TWO INSTRUMENTS
LTV	0.7	0.2	0.9	0.9
RW	0.2	-	0.3	0.3
ϕ_l	-	-	-	0.3
χ_τ	-	-	-	0.1
σ_l	17.7271	3.7614	16.4028	14.6057
σ_y	3.7178	3.3075	4.8729	4.6760
$\sigma_{(LTV+RW)}$	-	-	-	2.9762
Social welfare (losses/gains)	0.0002	-0.0032	0.0119	0.0162
Impatients (borrowers)	0.0409	-0.0005	0.1031	0.0863
Patients (savers)	-0.0390	-0.0060	-0.0717	-0.0494

Volatilities are expressed in %. The welfare metric used is the conditional welfare, computed conditionally on the initial state being the deterministic steady state of the model. The welfare losses/gains are expressed in terms of % of consumption equivalents. This is the same across policies. A second order approximation of the model is used for solving the model and providing those quantitative results.

Source: *Calculs BCL*.



Sources: *Calculs BCL*.

6.2 EFFECTS OF A MONETARY POLICY SHOCK UNDER OPTIMAL MACROPRUDENTIAL POLICIES

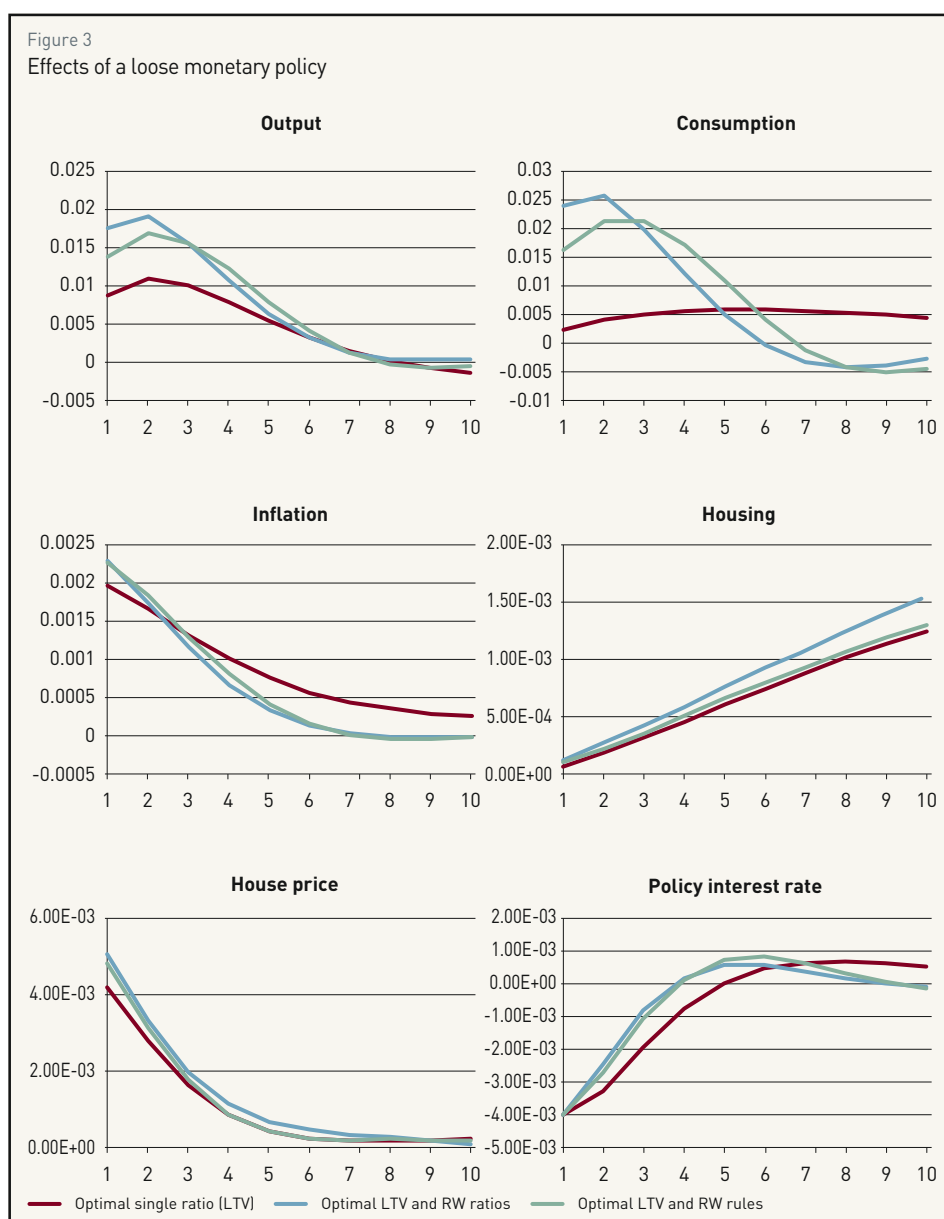
In order to understand the dynamics of the model and how the optimal LTV ratio interacts with the optimal RW, we simulate the impulse responses of the model using the optimal ratios and optimized parameters of the macroprudential rules we found in the previous section. We keep the estimated parameters of the model and supplement them with optimal ratios and parameters under the assumption of a loose monetary policy stance.

Figure 3 displays the expansionary effects of a 10 bps decrease in the monetary policy rate of the economy. This shock implies lower loan and effective borrowing rates. Consequently, mortgage

loans increase as along with overall mortgage debt stock, leading to an increase in the debt-to-GDP and debt-to-income ratios (except under the scenario with LTV ratio alone). The increase in mortgage loans supplied by banks positively impacts housing demand thereby increasing house prices. The rise in the house value generates an upswing of output and consumption. As the collateral constraint is binding with the LTV policy, the increase in mortgage loans is exacerbated following the increase in house value. Inflation increases following the decline in the policy rate and subsequently due to the increase in total consumption. Bank capital increases as a consequence of higher profits stemming from an upswing of economic activity and housing loans.

Comparing the impulse responses under different policy scenarios helps to provide some underlying economic intuition for the results discussed so far.

Figure 3 contrasts the optimal single ratio with the optimal two-instrument policy regime. As previously mentioned, mortgage credit flow is smoother under the single LTV policy case than the optimal two-instrument scenario. Therefore, debt-to-GDP and debt-to-income are decreasing



Source: *Calculs BCL*.

Note: Time, measured in quarters, is on the horizontal axis. All variables are measured in % deviations from steady state, except inflation and the interest rates which are measured in annualized deviations from steady state.

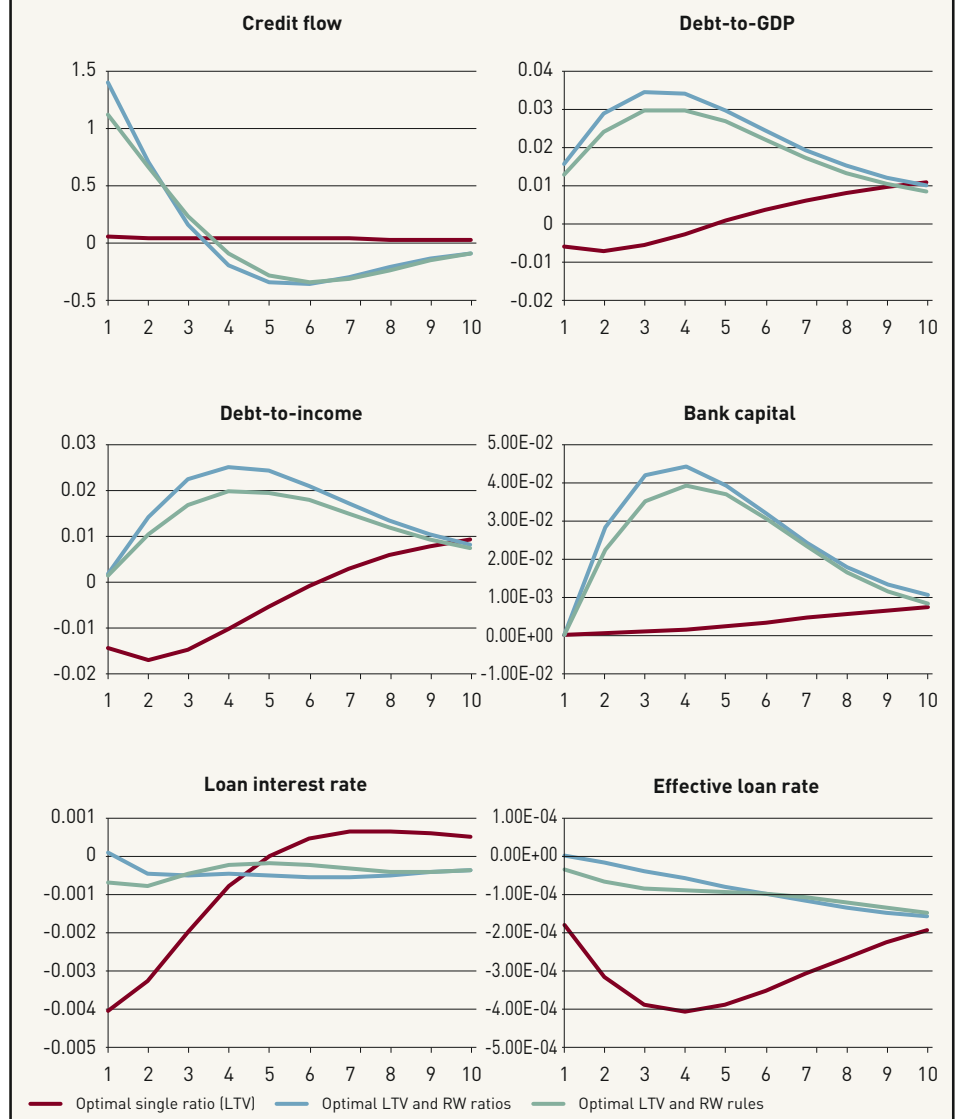
in the wake of the expansionary interest rate shock under the former while they go up in the latter where loans are more volatile and increase more. This channel affects all other variables in the economy. Indeed, house prices increase less in the case of the single LTV ratio scenario than in the case of the two-instrument scenario. Output increases more in the two-instrument policy compared to the single policy case. This is explained by agents' consumption pattern, which is subdued under the single policy regime due to a stronger mortgage loan restriction implied by a tight LTV ratio.

Overall, the differences between using LTV ratio alone and the two-instrument policy combination stem from the higher amount and volatility of loans in the latter policy scenario. As the optimal policy rules are not overly strict, Figure 3 shows that the paths of variables under that time varying policy scenario are close to those of the case of two-static ratios with the exception of the more stabilized mortgage credit, debt-to-GDP, debt-to-income and house prices under the time-varying policy rules scenario.

7 CONCLUSIONS


In this work, we try to assess the optimal macroprudential policy for LTV and RW macroprudential instruments in Luxembourg. To address this question, we build a DSGE model and estimate it on Luxembourg data using the Bayesian techniques. In comparison to the literature, our modelling approach assumes a monopolistically competitive banking sector, a collateral constraint and an explicit differentiation between the flow and the stock of household mortgage debt. We further contribute to the existing literature on this topic by identifying the optimal ratios and rules of the loan-to-value cap and the risk weighted capital requirement for Luxembourg. Specifically, we analyse the welfare effects of these instruments from a financial stability perspective and determine the optimal combination of borrower and capital based macroprudential instruments for Luxembourg.

Figure 4
Effects of a loose monetary policy



Source: *Calculs BCL.*

Note: Time, measured in quarters, is on the horizontal axis. All variables are measured in % deviations from steady state, except inflation and the interest rates which are measured in annualized deviations from steady state.



Based on a welfare analysis in the context of a loose monetary policy environment, we first find that the non-joint optimal individual LTV and RW ratios for Luxembourg seem to be 90% and 30%, respectively, while the joint optimal ratios are found at 100% and 10% respectively. We also find that combining LTV and RW measures welfare-dominates the use of LTV alone suggesting a possible complementarity between these instruments in terms of welfare. We note that the latter policy performs better than the former with respect to mortgage debt and house prices stabilization effects. This result suggests that the policy scenario that provides better stabilization effects on mortgage credits isn't necessarily the one that is welfare improving. In other words, LTV and RW measures can be considered as complements in terms of welfare, while their optimal combination diminishes the stabilization effects on mortgage debt and house prices. In particular, when LTV is applied alone in the context of an accommodative monetary environment, it is found to be too tight (i.e. 20%) to be realistic, leading to a welfare loss but helping to stabilize debt relative to the use of both LTV and RW ratios. In addition, the time-varying and endogenous LTV and RW rules improve overall social welfare and better stabilize the growth of mortgage loans and house prices relative to their static exogenous ratios. Finally, we find that the optimal interactions between LTV and RW ratios in our framework follow a convex shape. When LTV is increased, the corresponding optimal RW ratio is low and conversely when the RW ratio is increased, the corresponding optimal LTV ratio should be lowered.

In future work, we plan to extend the number and type of macroprudential instruments in the analysis by including amortization requirements and/or introducing debt-to-income (DTI)/debt service-to-income (DSTI) constraints in the model.

REFERENCES

- Albacete, N., Lindner, P. & Fessler, P. (2018), One policy to rule them all? on the effectiveness of LTV, DTI and DSTI ratio limits as macroprudential policy tools, Financial Stability Report (Austrian Central Bank) 35.
- Alpanda, S. & Zubairy, S. (2017), Addressing household indebtedness: monetary, fiscal or macroprudential policy?, *European Economic Review* 92, 47–73.
- Angelini, P., Neri, S. & Panetta, F. (2012), Monetary and macroprudential policies, European Central Bank, Working Paper No 1449/JULY 2012.
- Beneš, J., Laxton, D. & Mongardini, J. (n.d.), Mitigating the deadly embrace in financial cycles: counter-cyclical buffers and loan-to-value limits, IMF Working Paper No 16/87.
- Brooks, S. P. & Gelman, A. (1998), General methods for monitoring convergence of iterative simulations, *Journal of computational and graphical statistics* 7(4), 434–455.
- Brzoza-Brzezina, M., Kolasa, M. & Makarski, K. (2015), Macroprudential policy and imbalances in the euro area, *Journal of International Money and Finance* 51, 137–154.
- Brzoza-Brzezina, M., Kolasa, M. & Makarski, K. (2017), Monetary and macroprudential policy with foreign currency loans, *Journal of Macroeconomics* 54, 352–372.
- Calvo, G. A. (1983), Staggered prices in a utility-maximizing framework, *Journal of monetary Economics* 12(3), 383–398.

Chen, M. J. & Columba, M. F. (2016), Macroprudential and monetary policy interactions in a DSGE model for Sweden, IMF Working Paper No 16/74.

Deak, S., Fontagné, L., Maffezzoli, M. & Marcellino, M. (2011), LSM: a DSGE model for Luxembourg, *Economic modelling* 28(6), 2862–2872.

Fève, P., Pierrard, O. et al. (2017), Financial regulation and shadow banking: A small-scale DSGE perspective, Central Bank of Luxembourg, Working Paper Series No 111.

Galí, J. (2008), *Monetary policy, inflation, and the business cycle: an introduction to the new Keynesian framework*, Princeton University Press.

Galí, J. & Monacelli, T. (2005), Monetary policy and exchange rate volatility in a small open economy, *The Review of Economic Studies* 72(3), 707–734.

Galí, J. & Monacelli, T. (2008), Optimal monetary and fiscal policy in a currency union, *Journal of international economics* 76(1), 116–132.

Gambacorta, L. & Signoretti, F. M. (2014), Should monetary policy lean against the wind?: An analysis based on a DSGE model with banking, *Journal of Economic Dynamics and Control* 43, 146–174.

Gerali, A., Neri, S., Sessa, L. & Signoretti, F. M. (2010), Credit and banking in a DSGE model of the euro area, *Journal of Money, Credit and Banking* 42, 107–141.

Greenwald, D. (2018), The mortgage credit channel of macroeconomic transmission, MIT Sloan Research paper No.5184-16.

Grodecka, A. (2017), On the effectiveness of loan-to-value regulation in a multi-constraint framework, Sveriges Riksbank, Working Paper Series No 347/Nov 2017.

Guerrieri, L. & Iacoviello, M. (2017), Collateral constraints and macroeconomic asymmetries, *Journal of Monetary Economics* 90, 28–49.

Iacoviello, M. (2005), House prices, borrowing constraints, and monetary policy in the business cycle, *American economic review* 95(3), 739–764.

Iacoviello, M. & Neri, S. (2010), Housing market spillovers: evidence from an estimated DSGE model, *American Economic Journal: Macroeconomics* 2(2), 125–64.

Kannan, P., Rabanal, P. & Scott, A. M. (2012), Monetary and macroprudential policy rules in a model with house price booms, *The BE Journal of Macroeconomics* 12(1).

Kelly, R., McCann, F. & O’Toole, C. (2018), Credit conditions, macroprudential policy and house prices, *Journal of Housing Economics* 41, 153–167.

Kydland, F. E., Rupert, P. & Šustek, R. (2016), Housing dynamics over the business cycle, *International Economic Review* 57(4), 1149–1177.



Lubello, F. & Rouabah, A. (2017), Capturing macroprudential regulation effectiveness: A DSGE approach with shadow intermediaries, Central Bank of Luxembourg, Working Paper Series No 114.

Marchiori, L. & Pierrard, O. (2017), How does global demand for financial services promote domestic growth in Luxembourg? A dynamic general equilibrium analysis, *Economic Modelling* 62, 103–123.

Mendicino, C. & Punzi, M. T. (2014), 'House prices, capital inflows and macroprudential policy, *Journal of Banking & Finance* 49, 337–355.

Punzi, M. T. & Rabitsch, K. (2018), Effectiveness of macroprudential policies under borrower heterogeneity', *Journal of International Money and Finance* 85, 251–261.

Rubio, M. & Carrasco-Gallego, J. A. (2014), Macroprudential and monetary policies: Implications for financial stability and welfare, *Journal of Banking & Finance* 49, 326–336.

Sangaré, I. (2019), Housing sector and optimal macroprudential policy in an estimated DSGE model for Luxembourg, Mimeo.

Schmitt-Grohé, S. & Uribe, M. (2004), Solving dynamic general equilibrium models using a second-order approximation to the policy function', *Journal of economic dynamics and control* 28(4), 755–775.

Schmitt-Grohé, S. & Uribe, M. (2007), Optimal simple and implementable monetary and fiscal rules, *Journal of monetary Economics* 54(6), 1702–1725.